

changes, the induced stresses are expected to change accordingly and the critical points on the boundary will change as well.

### Elliptical opening

An elliptical opening is defined in Fig. 7.11 under field stresses  $\sigma_{\max}$  and  $\sigma_{\min}$ , where  $L_1 \parallel \sigma_{\min}$  and  $L_2 \parallel \sigma_{\max}$ . Based on elasticity theory, the tangential stress at critical Point A (or B, along the direction of  $\sigma_{\min}$ ) on the opening boundary is given by:

$$\sigma_{\theta A} = \sigma_{\max} (1 + 2 L_1/L_2 - k) \quad (7.14)$$

$$\text{or} \quad \sigma_{\theta A} = \sigma_{\max} (1 + \sqrt{2 L_1/r_A} - k) \quad (7.14a)$$

and at Point C (or D, along the direction of  $\sigma_{\max}$ ) is given by

$$\sigma_{\theta C} = \sigma_{\max} [k(1 + 2 L_2/L_1) - 1] \quad (7.15)$$

$$\text{or} \quad \sigma_{\theta C} = \sigma_{\max} [k(1 + \sqrt{2 L_2/r_C}) - 1] \quad (7.15a)$$

where  $r_A$  and  $r_C$  are the radii of curvature at A and C.

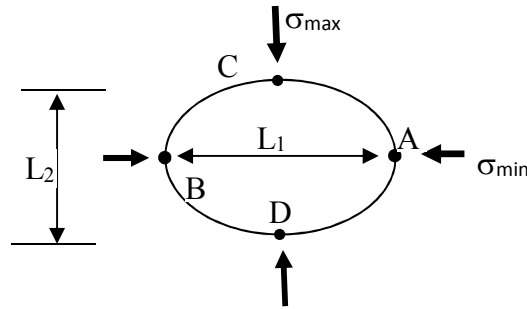


Fig. 7.11 Dimension of elliptical opening.

The above equations have in fact included Eqns. 7.12 and 7.13 for a circular opening if  $L_1 = L_2$  is used. Equations 7.14 and 7.15 include two important factors: the curvature at a corner, represented by radius  $r$  and the opening orientation, (represented by  $L_2/L_1$  ratio), relative to the major stress in the field. The effects of the two factors are examined below.